

# Motorway exit bridge 3D pushover analysis

Stéphane Commend, **GeoMod SA**

with the collaboration of **BG ingénieurs conseils SA**

# Contents

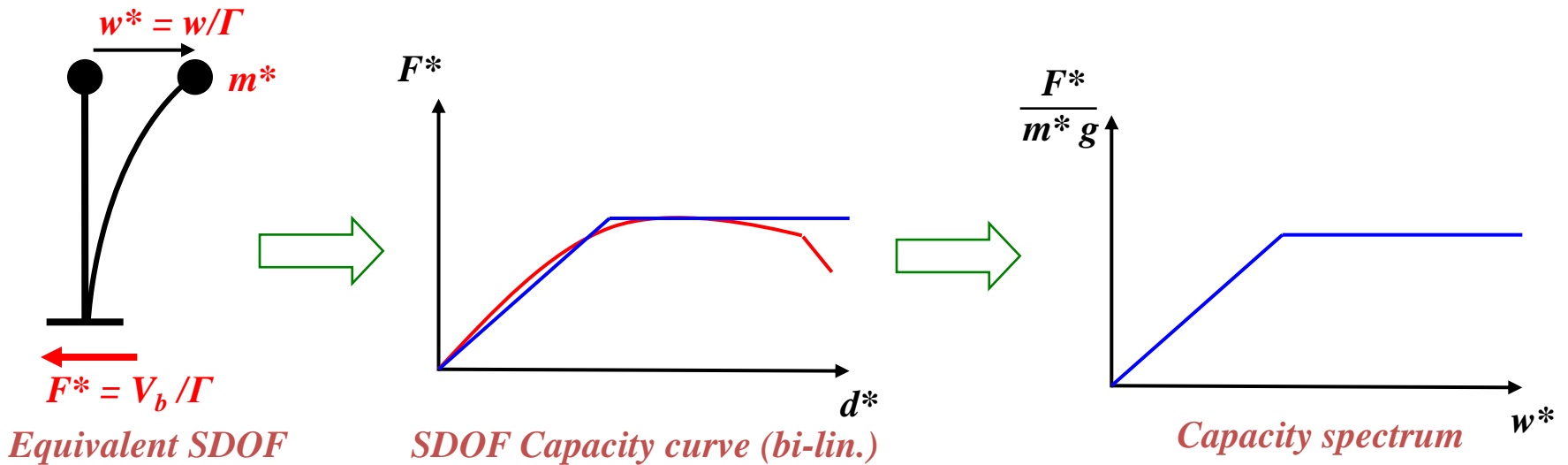
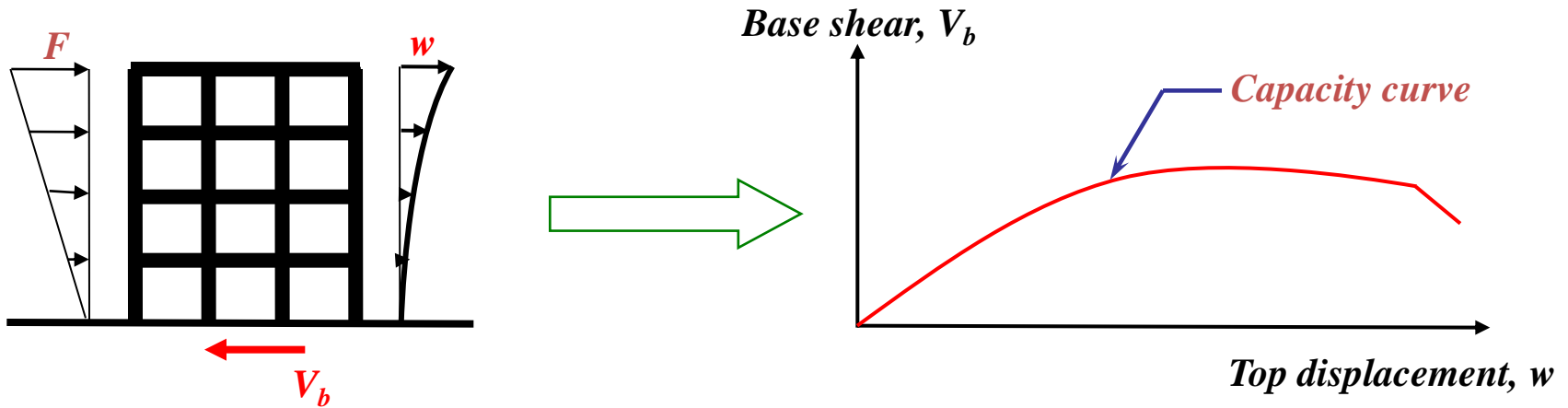
- Recall: push-over or displacement-based method
- 3D model of motorway exit
- Target displacement computation
- Deformation capacity
- Seismic assessment
- Conclusion

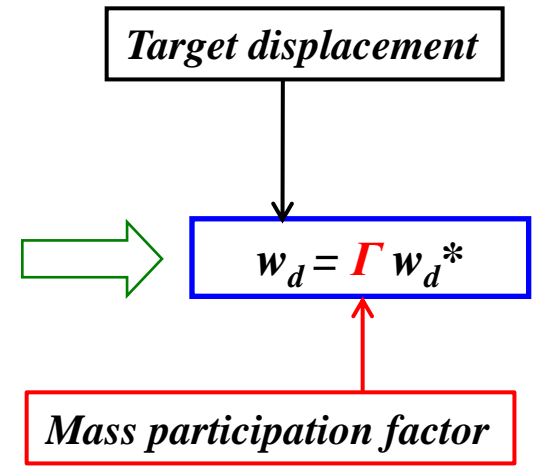
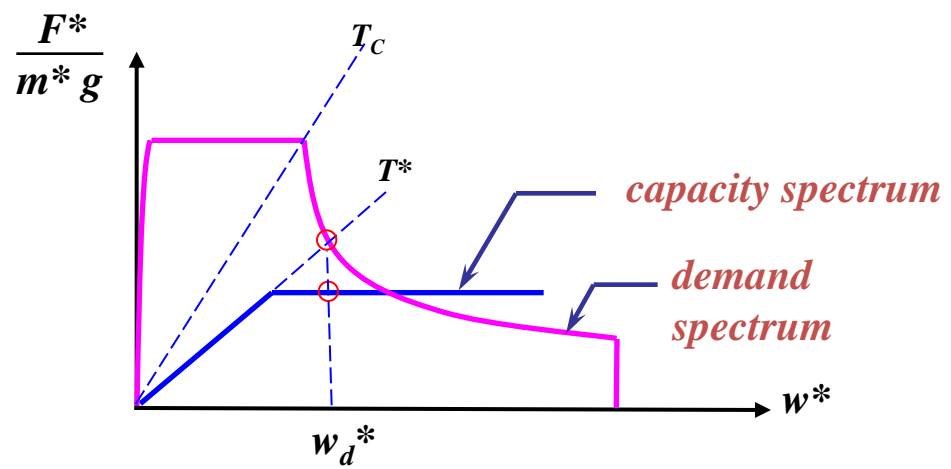
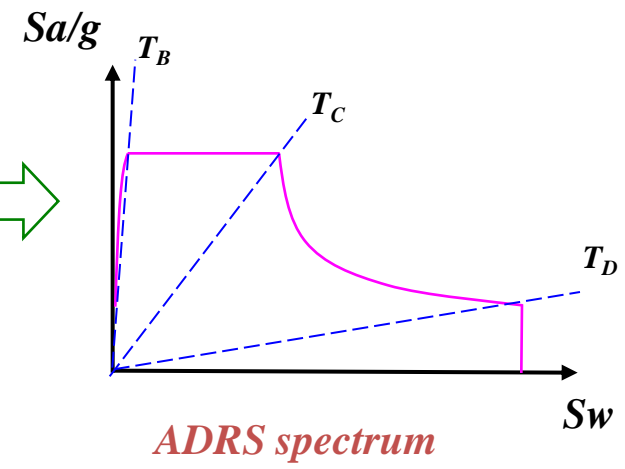
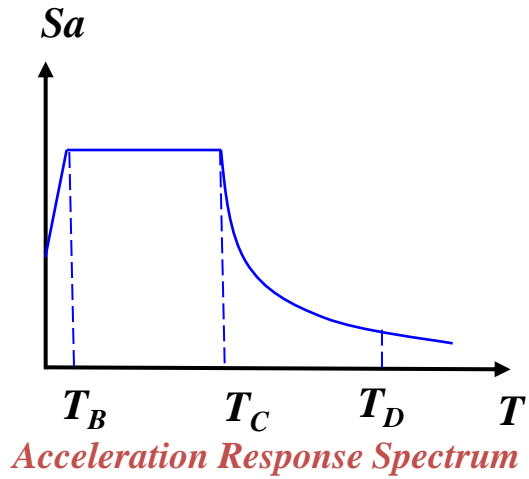
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# Seismic assessment of existing structures in Switzerland

- Classical methods: replacement forces, response spectra
- Since 2004: displacement-based method (push-over), documented in CT SIA 2018





$$\alpha_{\text{eff}} = W_{\text{Rd}} / W_{\text{d}} \quad (\text{SIA CT 2018})$$

$\alpha_{\text{eff}}$   
 $W_{\text{Rd}}$   
 $W_{\text{d}}$

### compliance factor

allowable displacement (capacity of deformation)  
 target displacement

$$\alpha_{\text{eff}} < \alpha_{\text{min}}$$

$$\alpha_{\text{min}} \leq \alpha_{\text{eff}} \leq \alpha_{\text{adm}}$$

$$\alpha_{\text{adm}} \leq \alpha_{\text{eff}}$$

intervention **necessary**

intervention **necessary, if proportionate**

**no intervention**

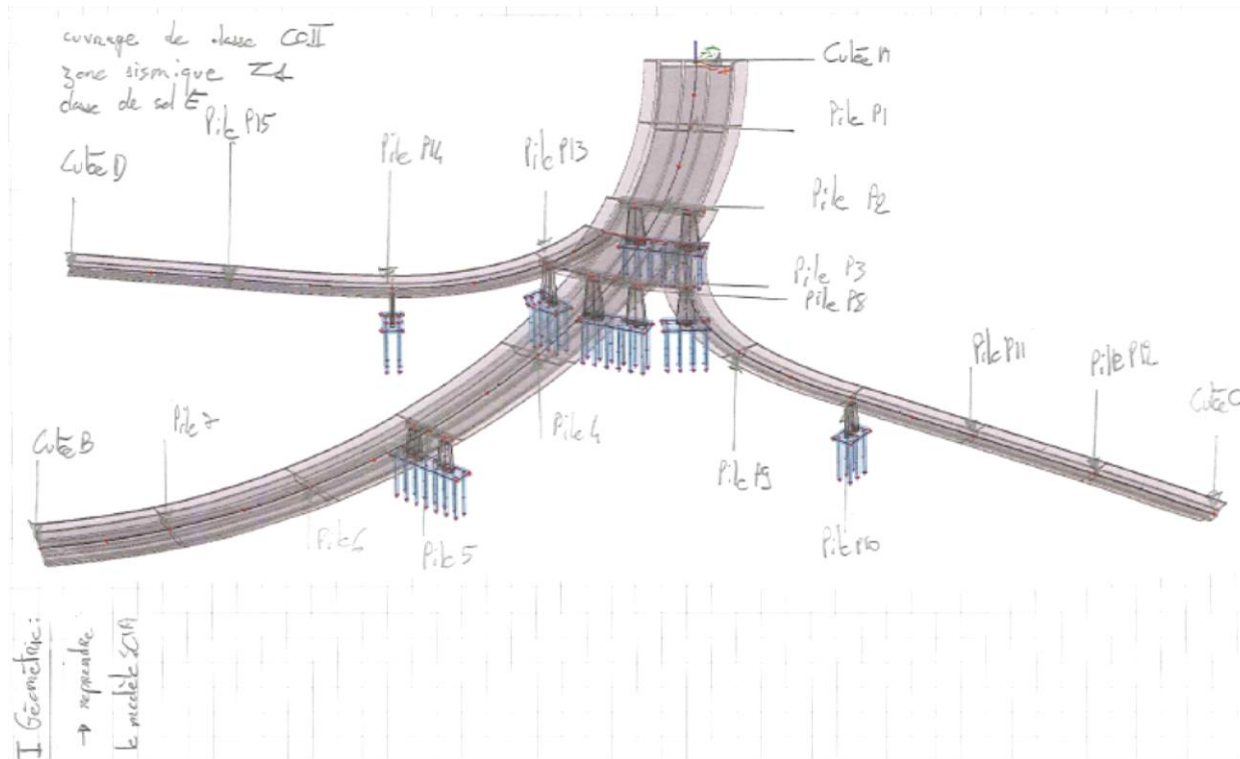
$\alpha_{\text{min}}, \alpha_{\text{adm}} = f(\text{structure type, lifetime})$

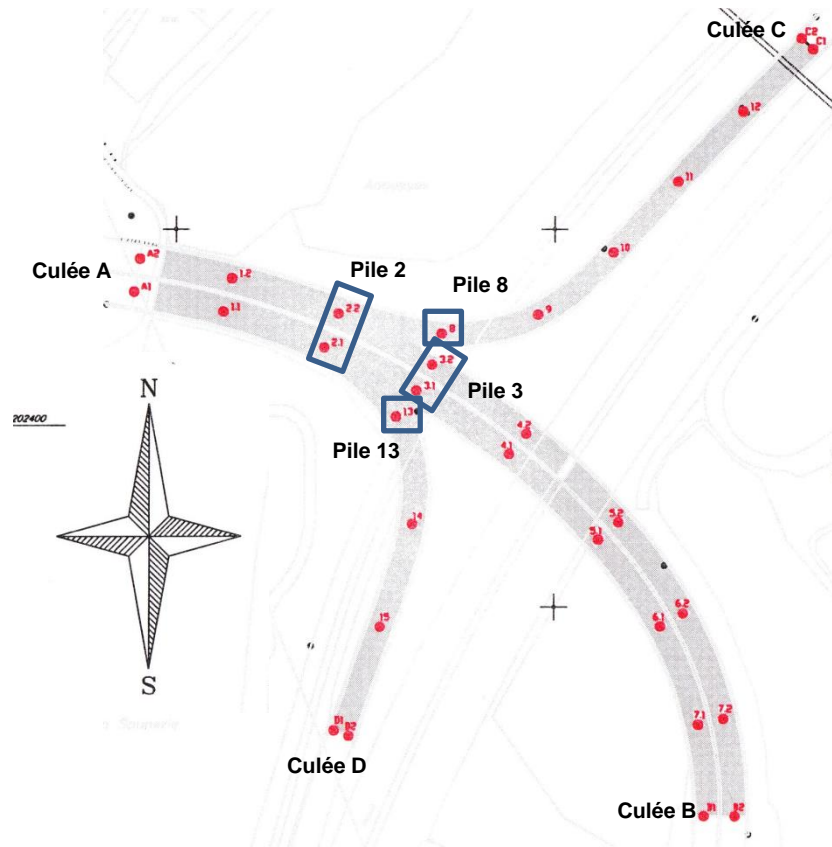
Here, for class II and T = 50 years:  $\alpha_{\text{min}} = 0.25$  et  $\alpha_{\text{adm}} = 0.76$

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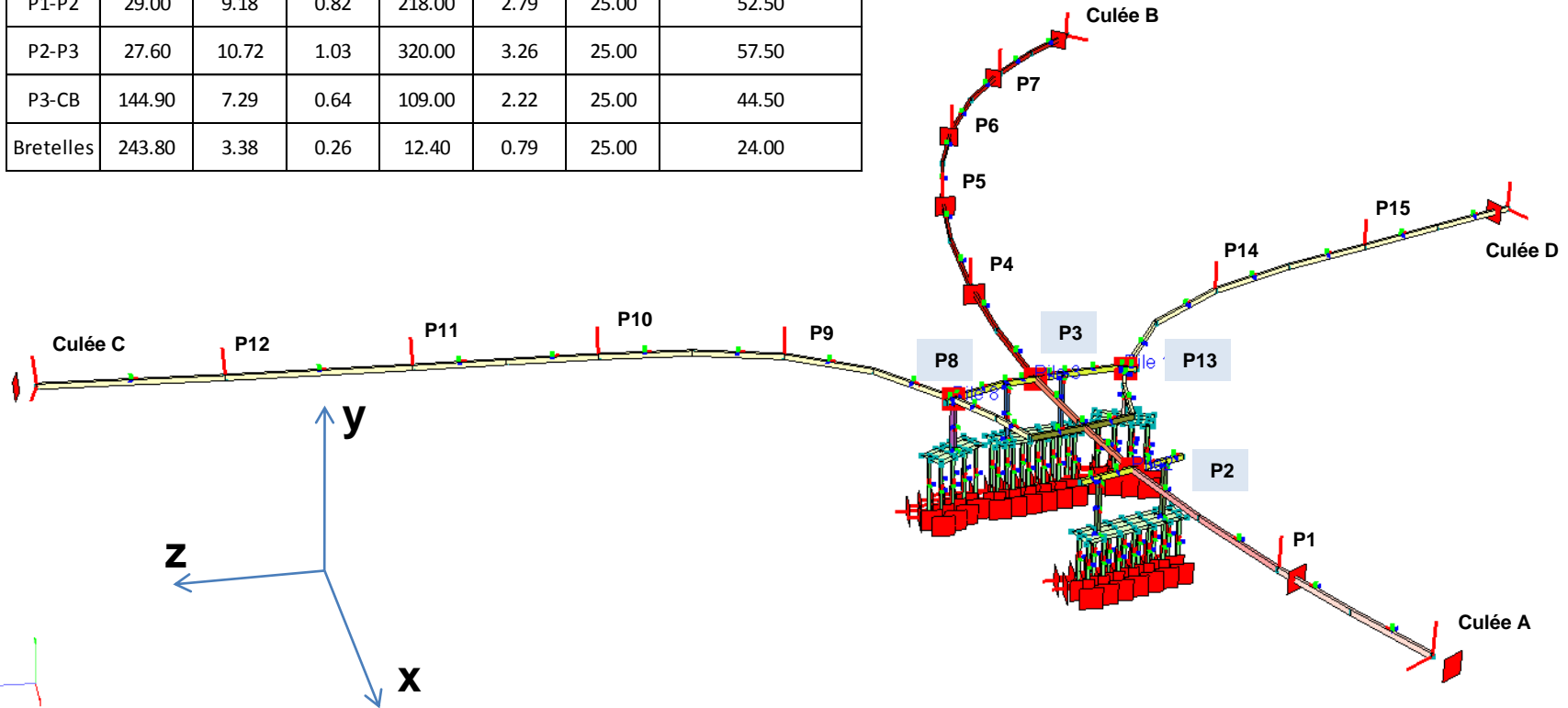






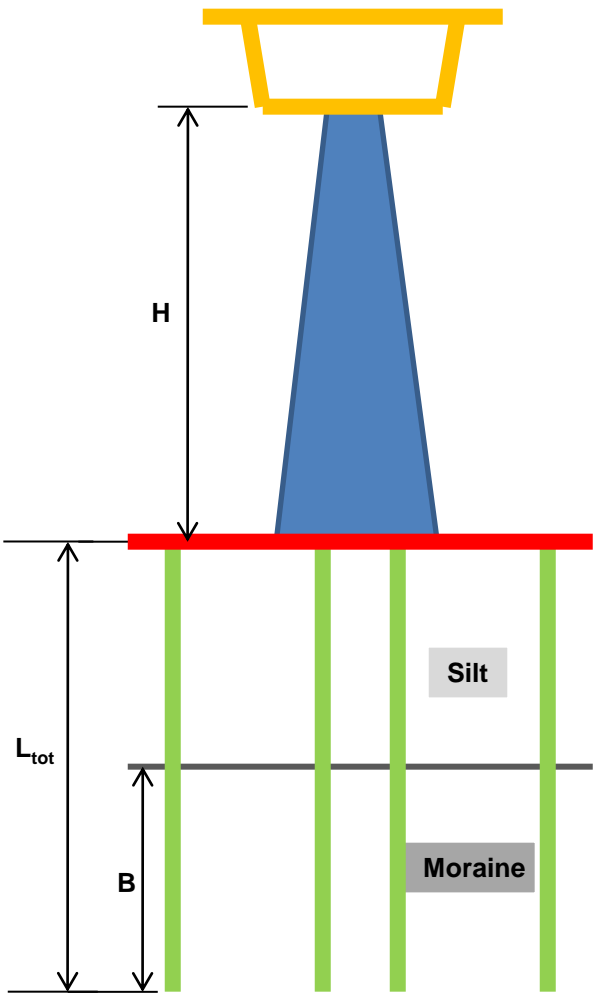
**Only P2 P3 P8 P13 are modeled explicitly**

| Caisson   | L      | A                 | lx                | ly                | lz                | $\gamma$             | q superstruct. |
|-----------|--------|-------------------|-------------------|-------------------|-------------------|----------------------|----------------|
|           | [m]    | [m <sup>2</sup> ] | [m <sup>4</sup> ] | [m <sup>4</sup> ] | [m <sup>4</sup> ] | [kN/m <sup>3</sup> ] | [kN/m]         |
| CA-P1     | 23.50  | 8.59              | 0.69              | 196.20            | 2.75              | 25.00                | 52.50          |
| P1-P2     | 29.00  | 9.18              | 0.82              | 218.00            | 2.79              | 25.00                | 52.50          |
| P2-P3     | 27.60  | 10.72             | 1.03              | 320.00            | 3.26              | 25.00                | 57.50          |
| P3-CB     | 144.90 | 7.29              | 0.64              | 109.00            | 2.22              | 25.00                | 44.50          |
| Bretelles | 243.80 | 3.38              | 0.26              | 12.40             | 0.79              | 25.00                | 24.00          |

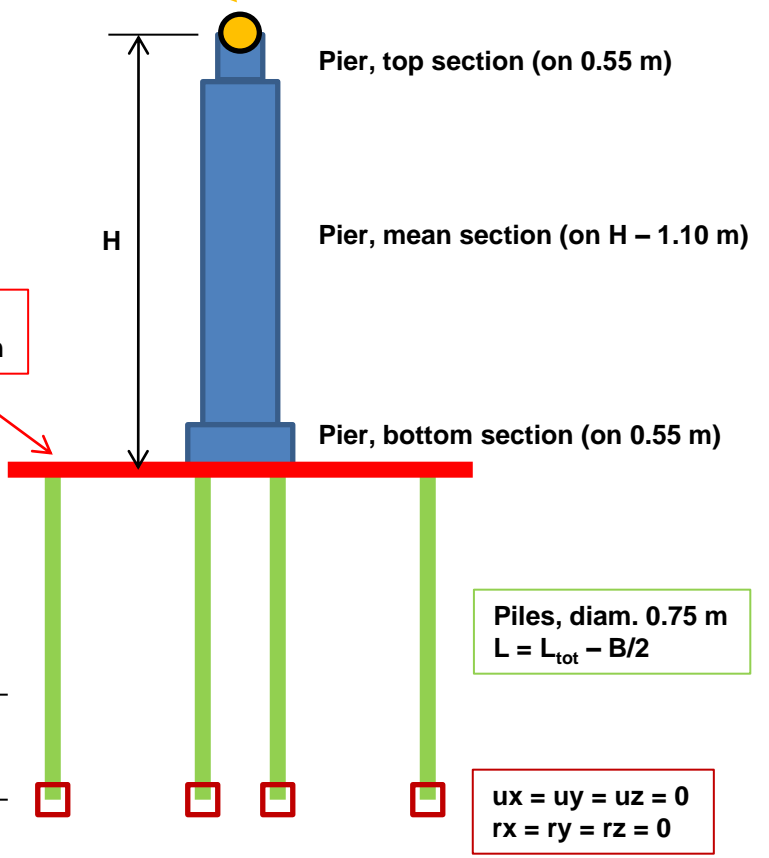


REAL LIFE

MODEL



Beam with characteristics as shown before

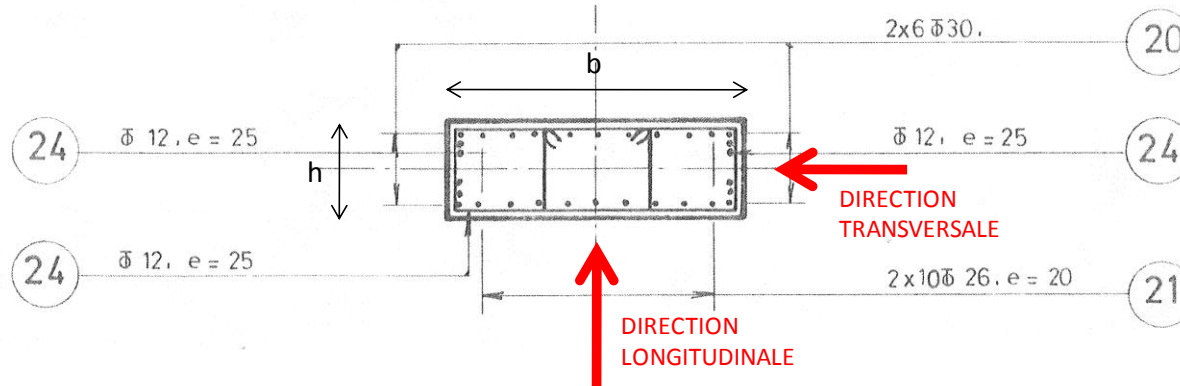


# Piers' characteristics

| Pile | modèle | H    | b top | h top | b moy | h moy | b bottom | h bottom |
|------|--------|------|-------|-------|-------|-------|----------|----------|
|      |        | [m]  | [mm]  | [mm]  | [mm]  | [mm]  | [mm]     | [mm]     |
| P2   | double | 8.05 | 2150  | 800   | 2825  | 800   | 3500     | 800      |
| P3   | double | 8.50 | 2150  | 800   | 2875  | 800   | 3600     | 800      |
| P8   | simple | 7.70 | 2050  | 800   | 2750  | 800   | 3450     | 800      |
| P13  | simple | 7.70 | 2050  | 800   | 2675  | 800   | 3300     | 800      |

| Elément                              | Modèle             | E       | $\nu$ | $\gamma$             | $f_c$                | $f_t$                |
|--------------------------------------|--------------------|---------|-------|----------------------|----------------------|----------------------|
|                                      |                    | [MPa]   | [-]   | [kN/m <sup>3</sup> ] | [kN/m <sup>2</sup> ] | [kN/m <sup>2</sup> ] |
| Pile (béton)                         | non linéaire       | 21'000  | 0.2   | 25                   | 30'000               | 2'500                |
| Pile (armatures)                     | non linéaire       | 210'000 | 0.3   | 78                   | 500'000              | 500'000              |
| Caissons, entretoises, pieux, dalles | élastique linéaire | 21'000  | 0.2   | 25                   | -                    | -                    |

# Piers' characteristics (cont.)



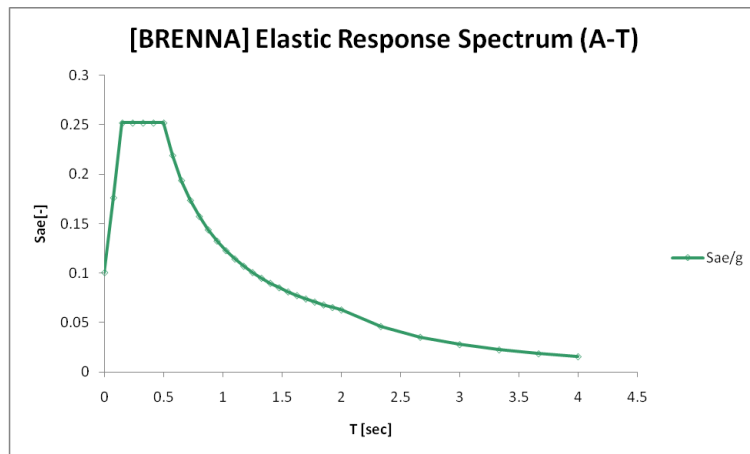
| Pile | Direction longitudinale |         |         |            | Direction transversale |        |        |          |
|------|-------------------------|---------|---------|------------|------------------------|--------|--------|----------|
|      | top                     | moy     | bottom  | étriers    | top                    | moy    | bottom | étriers  |
| P2   | 8phi26                  | 9phi26  | 13phi26 | 2xphi12e25 | 6phi30                 | 6phi30 | 6phi30 | phi12e25 |
| P3   | 9phi26                  | 10phi26 | 13phi30 | 2xphi12e25 | 6phi30                 | 6phi30 | 6phi30 | phi12e25 |
| P8   | 9phi26                  | 11phi26 | 13phi26 | 2xphi12e25 | 6phi26                 | 6phi26 | 6phi26 | phi12e25 |
| P13  | 9phi26                  | 10phi26 | 13phi26 | 2xphi12e25 | 6phi26                 | 6phi26 | 6phi26 | phi12e25 |

# Contents

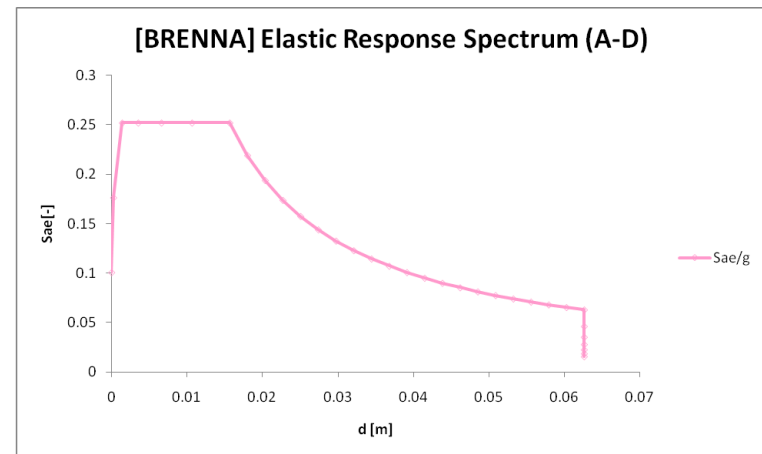
- Recall: push-over or displacement-based method
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# Demand spectrum

- Horizontal ground acceleration in Z1 :  $a_{gd} = 0.6 \text{ m/s}^2$
- Structure importance factor :  $\gamma_f = 1.2$
- Spectrum coefficient  $S = 1.4$
- Damping : 5 %



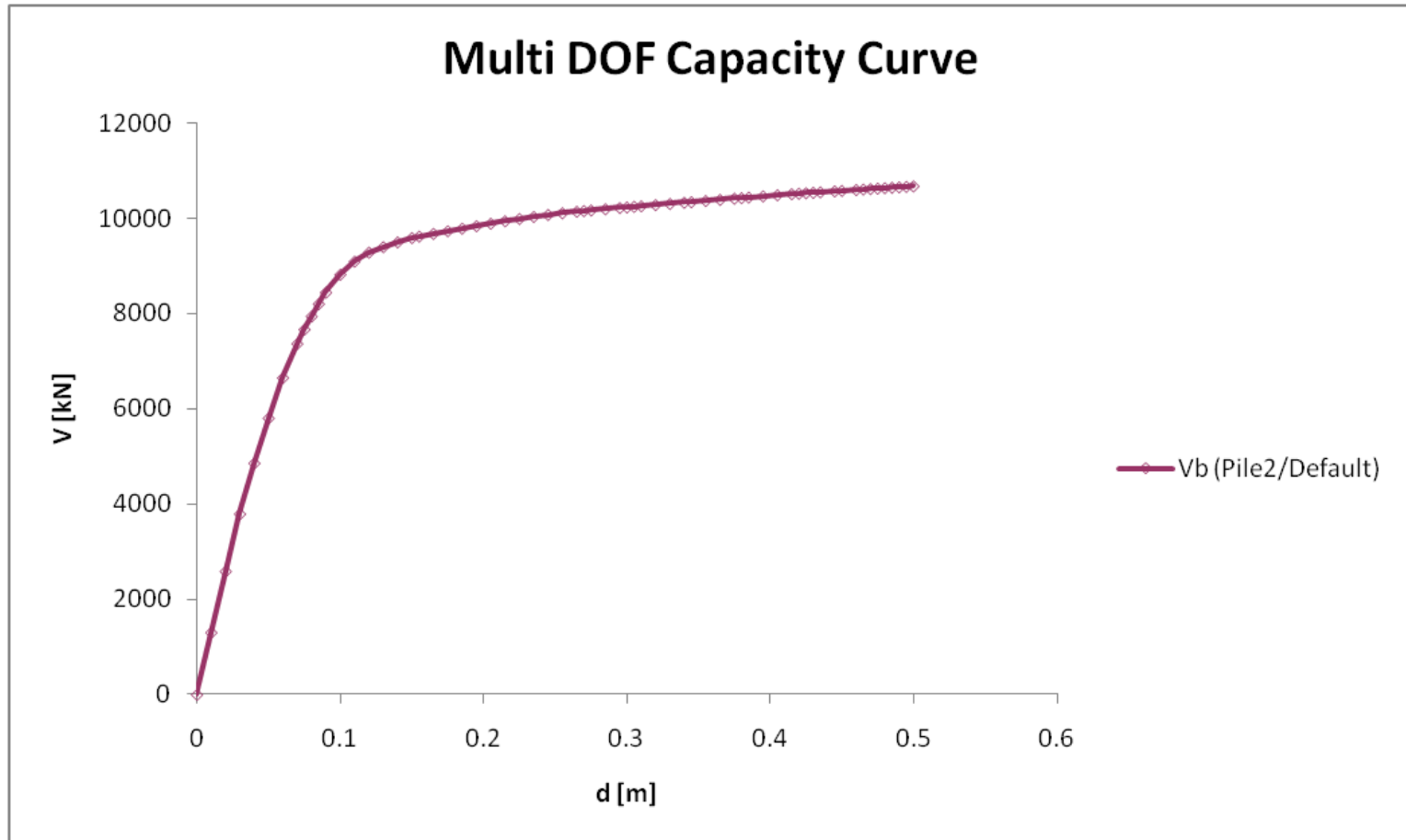
Acceleration response spectrum

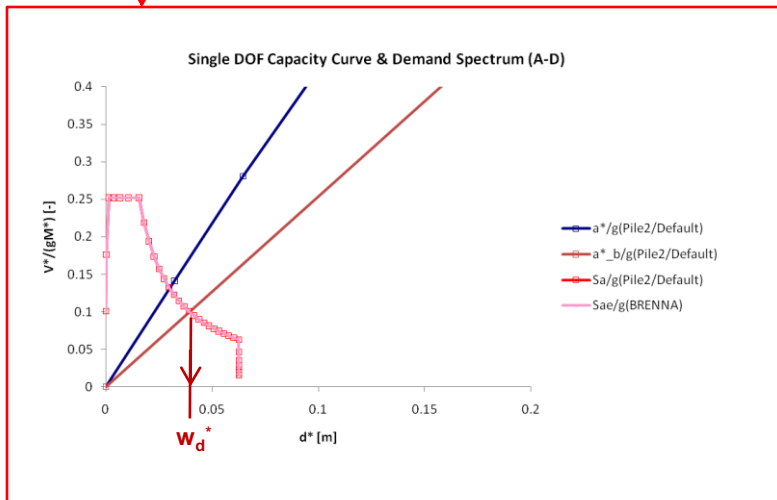
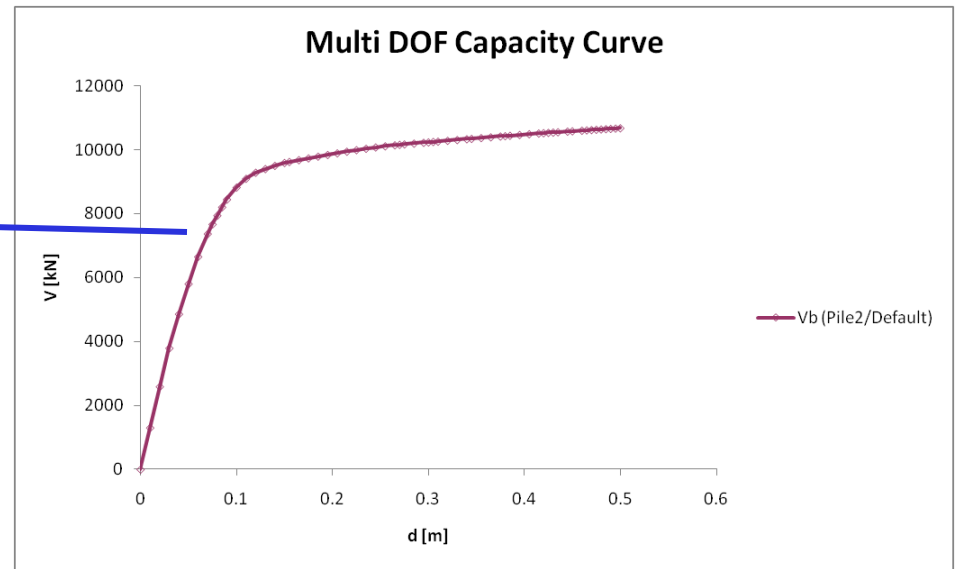
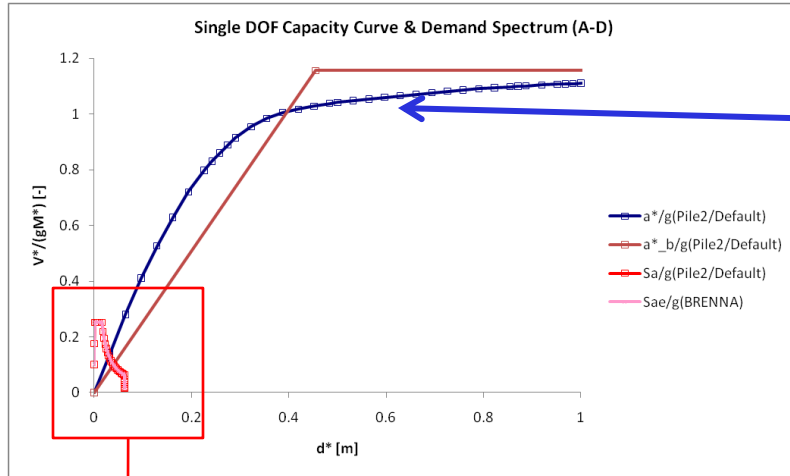


ADRS spectrum



# Capacity curve

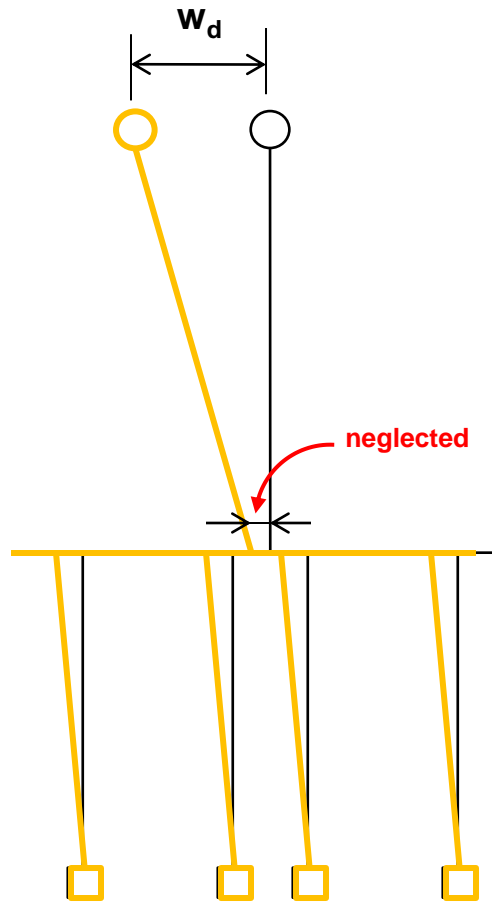




| Pushover analysis report        |        |               |
|---------------------------------|--------|---------------|
| Item                            | Unit   | Pile2/Default |
| MDOF Free vibr. period.....T    | [s]    | 1.64318       |
| SDOF Free vibr. period.....T*   | [s]    | 1.258785      |
| SDOF equivalent mass.....M*     | [kg]   | 3039220       |
| Mass participation factor Gamma | -      | 0.310006      |
| Bilinear yield force value..Fy* | [kN]   | 34449.4       |
| Bilinear displ. at yield....Dy* | [m]    | 0.454949      |
| Target displacement.....Dm*     | [m]    | 1.612872      |
| SDOF displacement demand....Dt* | [m]    | 0.039413      |
| Energy.....Em*                  | [kN*m] | 47726.1       |
| Reduction factor.....qu         | -      | 1             |
| Demand ductility factor.....mi  | -      | 40.9227       |
| Capacity ductility factor...miC | -      | 3.545169      |
| MDOF displacement demand.....Dt | [m]    | 0.012218      |

← w<sub>d</sub>\*

← w<sub>d</sub>



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$$W_{Rd} = \theta_{max} * L_v$$

$L_v$  : shear length =  $H/2$  for a fixed ended beam

Rotation capacity (simplified) :  $\theta_{max} = 3 * \theta_y$

Yielding chord rotation :  $\theta_y = \phi_y * L_v/3$

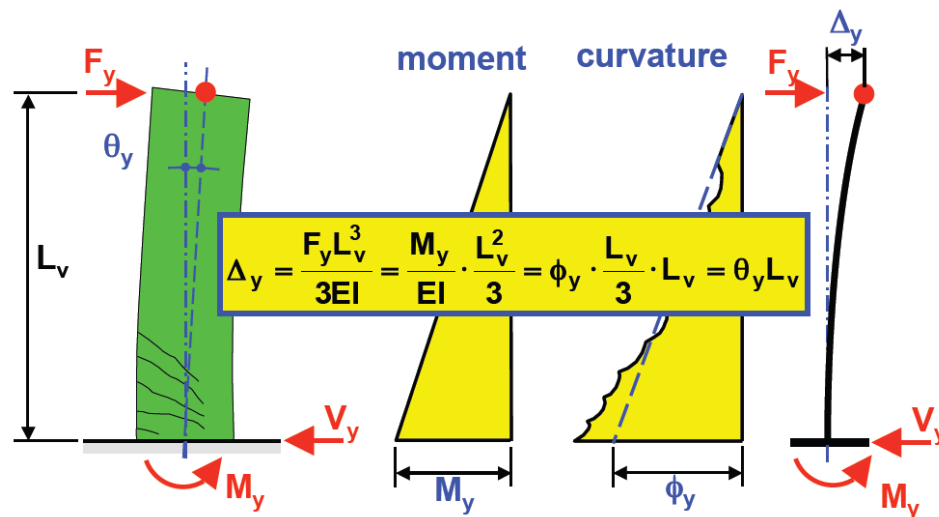
Plastification nominal curvature (simplified) :  $\phi_y = 2.1 * \epsilon_{sk}/h_b$

$\epsilon_{sk}$  : steel plastification strain = 0.2 %

$h_b$  : rectangular beam height

(see SIA CT 2018, 6.2)

### Yielding chord rotation $\theta_y$



© P. Lestuzzi, EPFL

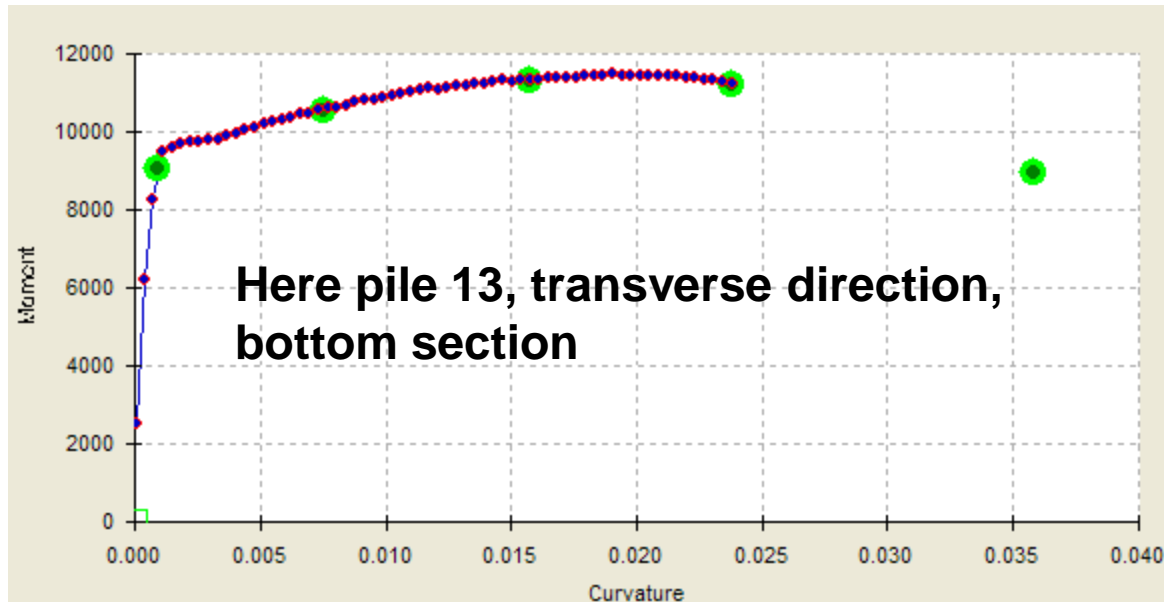
CIVIL-706 - displacement-based methods  
EPFL-ENAC-SGC 2005

-10-



# Shear stress verification

$M^+_{Rd,1}$  et  $M^+_{Rd,2}$  obtained with moment- curvature analysis



$$V_d^+ = (M^+_{Rd,1} + M^+_{Rd,2}) / H$$

# Shear stress verification

*Means that pier will fail due to shear before it reaches its maximal bending curvature*

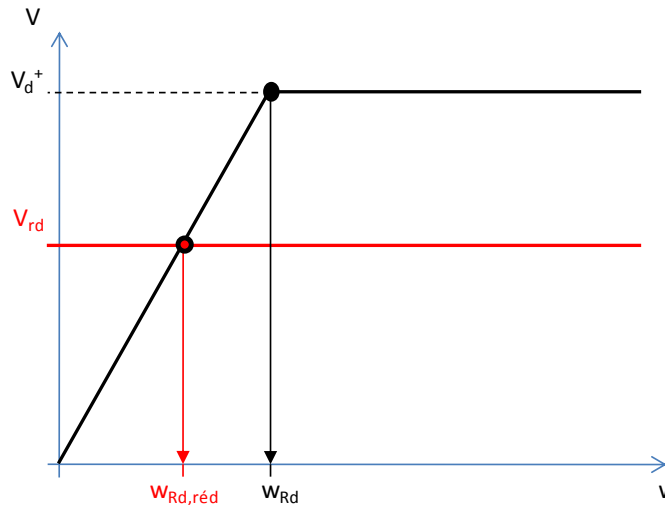
$$\text{When } V_d^+ > V_{Rd} \Rightarrow \alpha_{\text{eff,réd}} = W_{Rd,\text{réd}} / W_d$$

Nominal shear resistance

$$V_d^+ = (M_{Rd,1}^+ + M_{Rd,2}^+) / H$$

Maximal shear resistance

$$V_{rd} = A_{sw} / s * z * f_{sd} * \cot \alpha$$



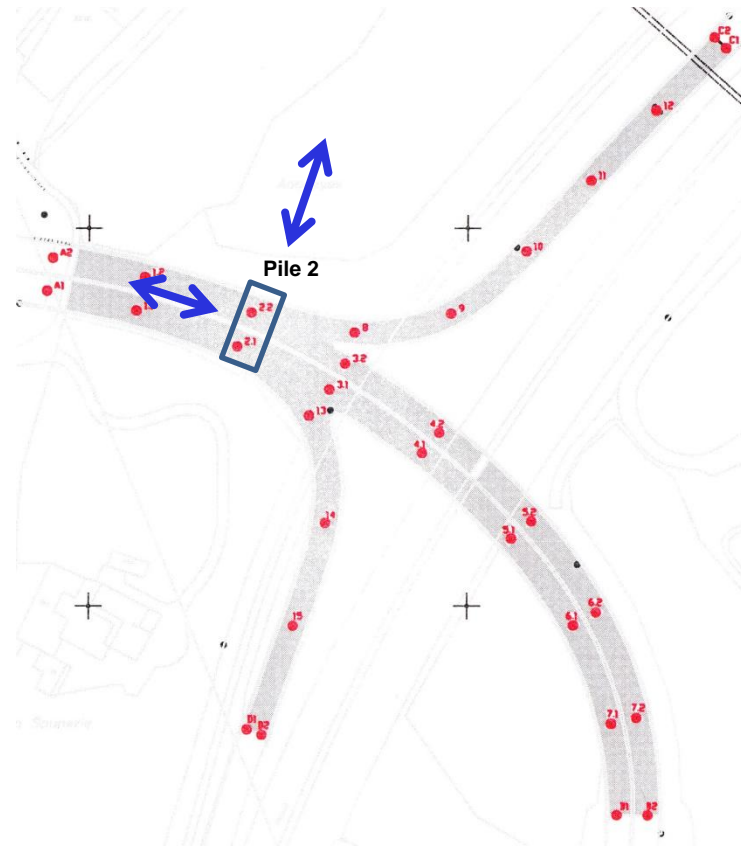
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For each pile (here pile 2), verification must be made:

- in **four directions** (+/- longitudinal, +/- transversal)
- for **two load distributions** (modal and unitary)



$$\alpha_{\text{eff}} = W_{\text{Rd}} / W_{\text{d}} \quad (\text{SIA CT 2018})$$

$\alpha_{\text{eff}}$   
 $W_{\text{Rd}}$   
 $W_{\text{d}}$

### compliance factor

allowable displacement (capacity of deformation)  
 target displacement

$$\alpha_{\text{eff}} < \alpha_{\text{min}}$$

$$\alpha_{\text{min}} \leq \alpha_{\text{eff}} \leq \alpha_{\text{adm}}$$

$$\alpha_{\text{adm}} \leq \alpha_{\text{eff}}$$

intervention **necessary**

intervention **necessary, if proportionate**

**no intervention**

$\alpha_{\text{min}}, \alpha_{\text{adm}} = f(\text{structure type, lifetime})$

Here, for class II and T = 50 years:  $\alpha_{\text{min}} = 0.25$  et  $\alpha_{\text{adm}} = 0.76$

| LONGI             |            |            |            |            |
|-------------------|------------|------------|------------|------------|
| PILE              | 2          | 3          | 8          | 13         |
| H [m]             | 8.05       | 8.5        | 7.7        | 7.7        |
| Lv [m]            | 4.025      | 4.25       | 3.85       | 3.85       |
| angle [°]         | 107        | 99         | 128        | 72         |
| dir_push_X        | -0.96      | -0.99      | -0.79      | -0.95      |
| dir_push_Z        | 0.29       | 0.16       | 0.62       | -0.31      |
| b_top [mm]        | 2150       | 2150       | 2050       | 2050       |
| b_mid [mm]        | 2825       | 2875       | 2750       | 2675       |
| b_bot [mm]        | 3500       | 3600       | 3450       | 3300       |
| h [mm]            | 800        | 800        | 800        | 800        |
| phi_L top         | 8phi26     | 9phi26     | 9phi26     | 9phi26     |
| phi_L mid         | 9phi26     | 10phi26    | 11phi26    | 10phi26    |
| phi_L bot         | 13phi26    | 13phi30    | 13phi26    | 13phi26    |
| Astop [mm2]       | 0.0042     | 0.0048     | 0.0048     | 0.0048     |
| Asmid [mm2]       | 0.0048     | 0.0053     | 0.0058     | 0.0053     |
| Asbot [mm2]       | 0.0069     | 0.0092     | 0.0069     | 0.0069     |
| phi_V             | 2xphi12e25 | 2xphi12e25 | 2xphi12e25 | 2xphi12e25 |
| VRd [kN]          | 1139       | 1139       | 1139       | 1139       |
| N top [kN]        | -3950      | -3550      | -2750      | -2850      |
| N bot [kN]        | -4400      | -4100      | -3150      | -3200      |
| MRd top [kNm]     | 2800       | 3200       | 2700       | 2700       |
| MRd bot [kNm]     | 4200       | 4700       | 3800       | 3700       |
| Vd [kN]           | 870        | 929        | 844        | 831        |
| d target mod [m]  | 0.0122     | 0.0115     | 0.0117     | 0.0068     |
| d target -mod [m] | 0.0123     | 0.0116     | 0.0117     | 0.0077     |
| d target 1 [m]    | 0.0120     | 0.0112     | 0.0117     | 0.0065     |
| d target -1 [m]   | 0.0120     | 0.0113     | 0.0117     | 0.0075     |
| phi_y             | 0.0053     | 0.0053     | 0.0053     | 0.0053     |
| w_y [m]           | 0.0284     | 0.0316     | 0.0259     | 0.0259     |
| w_Rd [m]          | 0.0851     | 0.0948     | 0.0778     | 0.0778     |
| alpha mod         | 6.97       | 8.25       | 6.65       | 11.44      |
| alpha -mod        | 6.91       | 8.17       | 6.65       | 10.11      |
| alpha 1           | 7.09       | 8.47       | 6.65       | 11.97      |
| alpha -1          | 7.09       | 8.39       | 6.65       | 10.38      |

| TRANS             |          |          |          |          |
|-------------------|----------|----------|----------|----------|
| PILE              | 2        | 3        | 8        | 13       |
| H [m]             | 8.05     | 8.5      | 7.7      | 7.7      |
| Lv [m]            | 4.025    | 4.25     | 3.85     | 3.85     |
| angle [°]         | 107      | 99       | 128      | 72       |
| dir_push_X        | -0.29    | -0.16    | -0.62    | 0.31     |
| dir_push_Z        | -0.96    | -0.99    | -0.79    | -0.95    |
| h_top [mm]        | 2150     | 2150     | 2050     | 2050     |
| h_mid [mm]        | 2825     | 2875     | 2750     | 2675     |
| h_bot [mm]        | 3500     | 3600     | 3450     | 3300     |
| b [mm]            | 800      | 800      | 800      | 800      |
| phi_L top         | 6phi30   | 6phi30   | 6phi26   | 6phi26   |
| phi_L mid         | 6phi30   | 6phi30   | 6phi26   | 6phi26   |
| phi_L bot         | 6phi30   | 6phi30   | 6phi26   | 6phi26   |
| Astop [mm2]       | 0.0042   | 0.0042   | 0.0032   | 0.0032   |
| Asmid [mm2]       | 0.0042   | 0.0042   | 0.0032   | 0.0032   |
| Asbot [mm2]       | 0.0042   | 0.0042   | 0.0032   | 0.0032   |
| phi_V             | phi12e25 | phi12e25 | phi12e25 | phi12e25 |
| VRd top [kN]      | 1595     | 1595     | 1519     | 1519     |
| N top [kN]        | -3950    | -3550    | -2750    | -2850    |
| N bot [kN]        | -4400    | -4100    | -3150    | -3200    |
| MRd top [kNm]     | 8800     | 8200     | 6300     | 6400     |
| MRd bot [kNm]     | 15800    | 16000    | 11600    | 11200    |
| Vd [kN]           | 3056     | 2847     | 2325     | 2286     |
| d target mod [m]  | 0.0018   | 0.0033   | 0.0060   | 0.0049   |
| d target -mod [m] | 0.0018   | 0.0033   | 0.0073   | 0.0049   |
| d target 1 [m]    | 0.0017   | 0.0028   | 0.0052   | 0.0038   |
| d target -1 [m]   | 0.0019   | 0.0028   | 0.0062   | 0.0038   |
| phi_y bot         | 0.0012   | 0.0012   | 0.0012   | 0.0013   |
| w_y [m]           | 0.0065   | 0.0070   | 0.0060   | 0.0063   |
| w_y_red [m]       | 0.0034   | 0.0039   | 0.0039   | 0.0042   |
| w_Rd_red [m]      | 0.0101   | 0.0118   | 0.0118   | 0.0125   |
| alpha mod red     | 5.64     | 3.58     | 1.97     | 2.56     |
| alpha -mod red    | 5.64     | 3.58     | 1.62     | 2.56     |
| alpha 1 red       | 5.97     | 4.22     | 2.27     | 3.30     |
| alpha -1 red      | 5.34     | 4.22     | 1.90     | 3.30     |

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| distribution<br>selon §3.6 | Direction longitudinale: $\alpha_{eff} = wRd / wd$ |          |          |            | Direction transversale: $\alpha_{eff} = wRd, r\acute{e}d / wd$ |          |          |            |
|----------------------------|--|----------|----------|------------|--|----------|----------|------------|
|                            | modale   | - modale | uniforme | - uniforme | modale   | - modale | uniforme | - uniforme |
| Pile 2                     | 6.97   | 6.91     | 7.09     | 7.09       | 5.64   | 5.64     | 5.97     | 5.34       |
| Pile 3                     | 8.25   | 8.17     | 8.47     | 8.39       | 3.58   | 3.58     | 4.22     | 4.22       |
| Pile 8                     | 6.65   | 6.65     | 6.65     | 6.65       | 1.97   | 1.62     | 2.27     | 1.90       |
| Pile 13                    | 11.44  | 10.11    | 11.97    | 10.38      | 2.56   | 2.56     | 3.30     | 3.30       |

**Seismic assesment OK because  $\alpha_{eff} \geq \alpha_{adm} = 0.76$   
for each pile in each direction**

# Why use displacement-based method instead of classical replacement forces method?



**Design horizontal acceleration in the 1960s-1970s: small**  
**Verification in the 2000s:  $a_h \gg ! \Rightarrow$  RF often fails !**  
**RF method: behavior coefficient  $q \Rightarrow$  hidden reserves...**

|                        |              |           |       |           | Coefficient de conformité $\alpha$ (réduit à $\alpha_{red}$ si nécessaire) pour chaque pile |      |       |       |       |       |       |       |       |
|------------------------|--------------|-----------|-------|-----------|---|------|-------|-------|-------|-------|-------|-------|-------|
|                        |              |           | T [s] | $S_d$ [%] | 1 VD  | 1 FR | 2 VD  | 2 FR  | 3 VD  | 3 FR  | 4 VD  | 4 FR  | 5     |
| Forces de remplacement | transversal  | encastré  | 1.9   | 5.6       | 10.19   | 1.10 | 2.95  | 3.19  | 2.93  | 2.77  | 1.94  | 1.94  | 6.46  |
|                        |              | base      | 2.2   | 4.9       | -   | -    | -     | -     | -     | -     | -     | -     | -     |
|                        |              | optimiste | 2.2   | 4.9       | -   | -    | -     | -     | -     | -     | -     | -     | -     |
|                        | longitudinal | encastré  | 0.8   | 13.0      | 0.21  | 0.23 | 4.96  | 4.86  | 4.36  | 4.89  | 1.86  | 1.64  | 0.56  |
|                        |              | base      | 1.4   | 7.6       | 0.25  | 0.49 | 6.49  | 8.44  | 7.06  | 8.66  | 1.17  | 1.49  | 3.41  |
|                        |              | optimiste | 1.8   | 5.2       | 0.46  | 1.53 | 9.53  | 13.14 | 11.00 | 14.36 | 1.48  | 1.91  | 4.41  |
| Push-over              | transversal  | encastré  | 1.9   | 5.6       | 23.57   | 3.16 | 17.67 | 21.67 | 19.24 | 16.50 | 24.03 | 31.59 | 95.75 |
|                        |              | base      | 2.2   | 4.9       | -   | -    | -     | -     | -     | -     | -     | -     | -     |
|                        |              | optimiste | 2.2   | 4.9       | -   | -    | -     | -     | -     | -     | -     | -     | -     |
|                        | longitudinal | encastré  | 0.8   | 13.0      | 0.20  | 0.18 | 38.66 | 51.25 | 50.90 | 41.24 | 8.29  | 7.31  | 1.61  |
|                        |              | base      | 1.4   | 7.6       | 0.38  | 0.36 | 33.20 | 34.19 | 42.58 | 43.83 | 7.58  | 8.42  | 1.77  |
|                        |              | optimiste | 1.8   | 5.2       | 0.76  | 0.76 | 29.91 | 30.74 | 38.82 | 39.88 | 6.89  | 7.63  | 2.97  |

Compliance factor always >  $\alpha_{adm}$  !

encastré: encastrement de toutes les piles à la jonction pile-puits,  $a_{gd} = 1 \text{ m/s}^2$ , inclinaison des bielles à 45°  
base: encastrement de toutes les piles à - 12 m sous la jonction pile-puits,  $a_{gd} = 1 \text{ m/s}^2$ , inclinaison des bielles à 45°  
optimiste: encastrement de la pile 1 à - 18 m au lieu de - 12 m,  $a_{gd} = 0.83 \text{ m/s}^2$  au lieu de  $1 \text{ m/s}^2$ , inclinaison des bielles à 25°

$\alpha < \alpha_{min} = 0.25$   
 $\alpha_{min} = 0.25 < \alpha < \alpha_{adm,50} = 0.76$