

# Time history dynamic analyses of geotechnical structures



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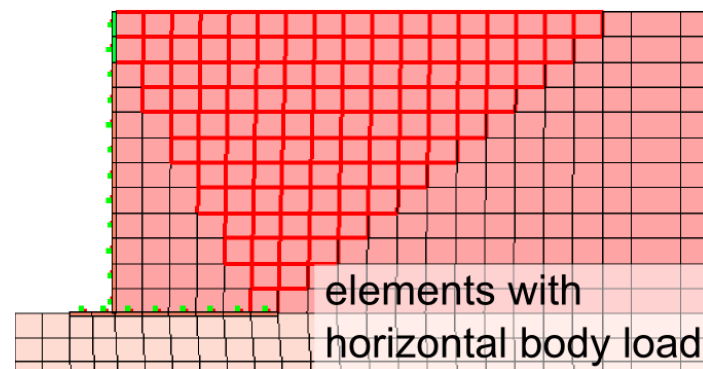
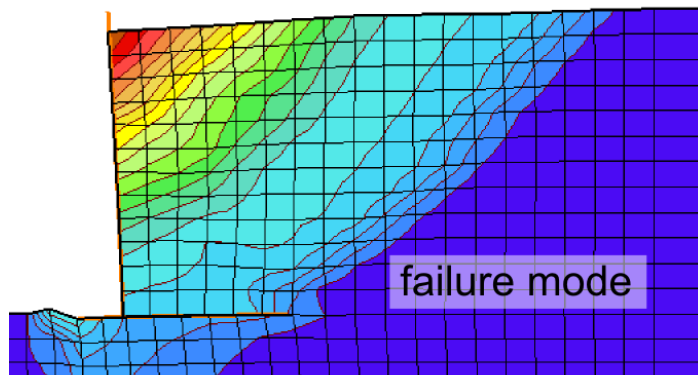
ZSoil® 2013

# Overview

- Retaining walls
  - Current practice in CH (within GeoMod, norms)
  - Comparison replacement force (RF) method - time history (TH)
- > RF method is overly conservative
- > TH on 2D model can be good alternative

# Retaining walls: Norm SIA 261 & 267(proposed)

- Replacement force method:
  - Applied to structure and part of adjacent soil, corresponding to failure mechanism (SIA267§7.4)



# Retaining walls: Norm SIA 261 & 267(proposed)

- Replacement force method:

– Force: 
$$A_{h,d} = \gamma_f \frac{a_{g,d}}{g q_a q_h} \cdot S \cdot G_K$$

$\gamma_f$ : Importance

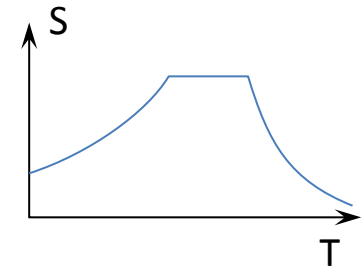
$a_{g,d}/g$ : Ground acceleration

$q_a$  &  $q_h$ : Coefficients accounting for ductility and spatial extension/variability

1.0 - 2.0      ~1.0

S: Design spectrum -> generally plateau value

$G_K$ : Mass



# Retaining walls: Norm SIA 261 & 267(proposed)

- Replacement force method:

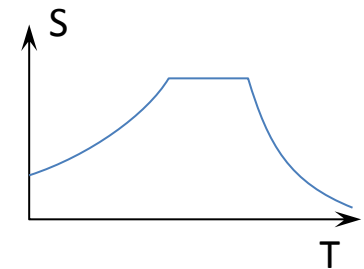
– Force: 
$$A_{h,d} = \gamma_f \frac{a_{g,d}}{g q_a q_h} \cdot S \cdot G_K$$

- Leads to very conservative design!
- No useful for estimating deformation

$\gamma_f$ : Importance  
 $a_{g,d}/g$ : Ground acceleration  
 $q_a$  &  $q_h$ : Coefficients accounting for ductility and spatial extension/variability

1.0 - 2.0      ~1.0

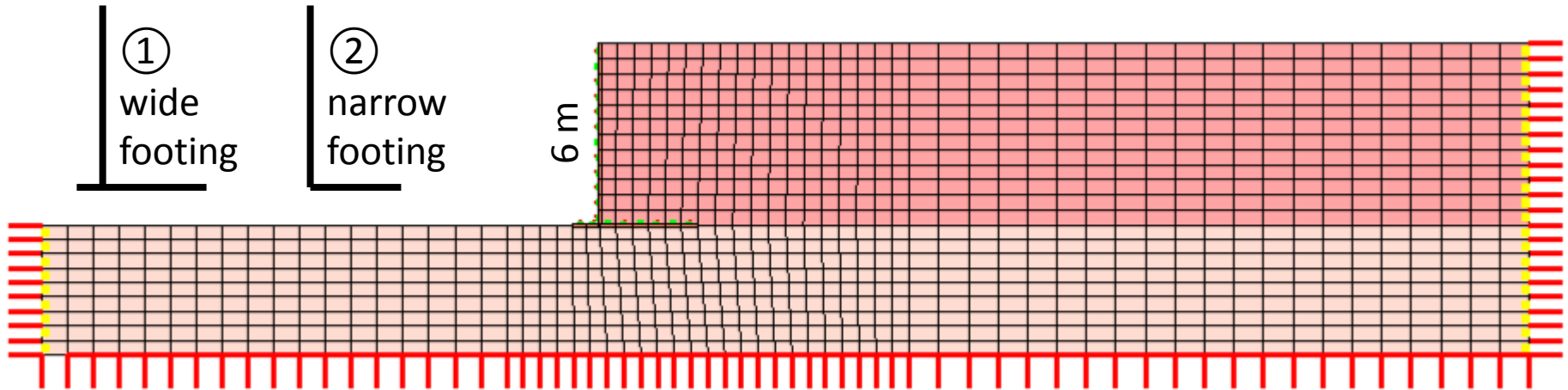
$S$ : Design spectrum -> generally plateau value  
 $G_K$ : Mass



# Non-linear analysis in time domain

- Not covered in SIA or EC (some guidelines exist for e.g. dams and highway infrastructures)
- Guidelines in e.g. Kramer, Geotechnical Earthquake Engineering, 1996.
  - Discretization (time, space)
  - Boundary conditions (free/fixed, absorbing, more advanced methods)
- Zsoil report (Menu Help->Reports->Dynamics)
- Topic of active research

# FE-Model of retaining wall



- Rigid base, horizontal seismic motion applied by changing reference frame:

$$M\ddot{x} + C\dot{x} + Kx = F \quad \Rightarrow \quad \ddot{x} = \ddot{x}_{rel} + \ddot{x}_g \quad \Rightarrow \quad M\ddot{x}_{rel} + C\dot{x} + Kx = F - M\ddot{x}_g$$

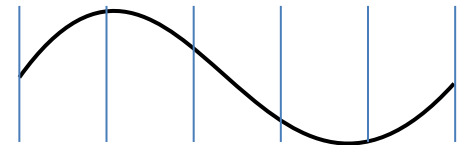
- Absorbing lateral boundaries

# Discretization

- **Mesh size:** 5-10 nodes per shortest wavelength

$$h^e \leq \frac{\lambda_{min}}{\{5 - 10\} \cdot v_s}$$

$$\lambda_{min} = \frac{v_s}{f_{max}}$$



where  $f_{max}$  depends on the application. For typical seismic records  $f_{max} = 10-20$  Hz.

- **Time step length:** 5-10 steps per shortest period

$$\Delta t \leq \frac{h^e}{v_s}$$

or, a wave should not travel through more than one *element per time step*



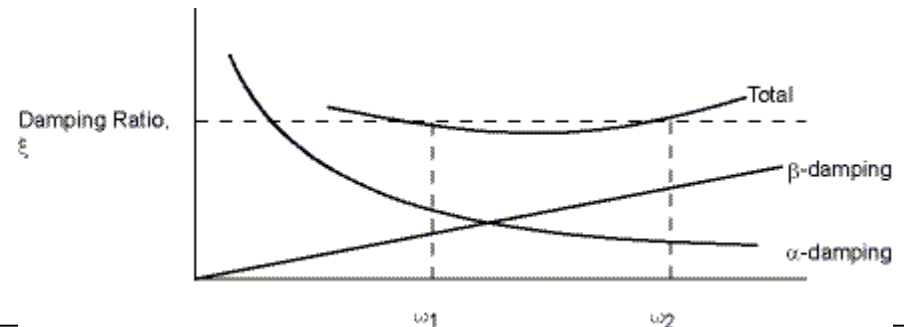


# Algorithm & Damping

- Distinguish between physical and numerical damping
- Physical damping in the model:
  - Energy dissipation:
    - Plasticity
    - Nonlinear elasticity (HSS)
  - Absorbing boundaries: Simulate radiation damping

# Algorithm & Damping (cont.)

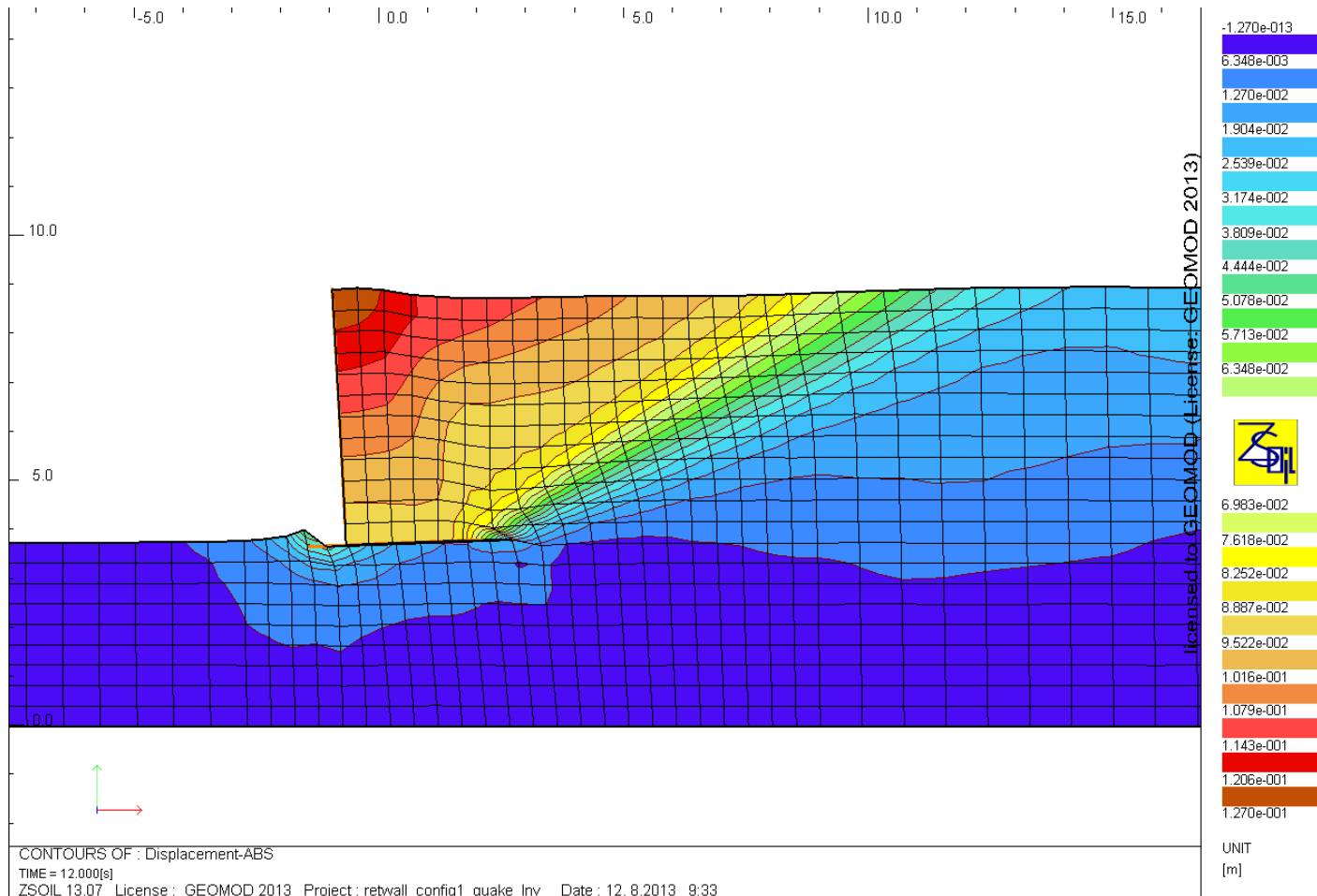
- Use HHT-Algorithm to numerically damp/eliminate high frequencies (noise)
- Rayleigh damping:
  - Small amount can be necessary for numerical reasons
  - Careful with mass-proportional damping ( $\alpha_0$  in ZSoil): Low frequencies are excessively damped!



# Interpretation of results

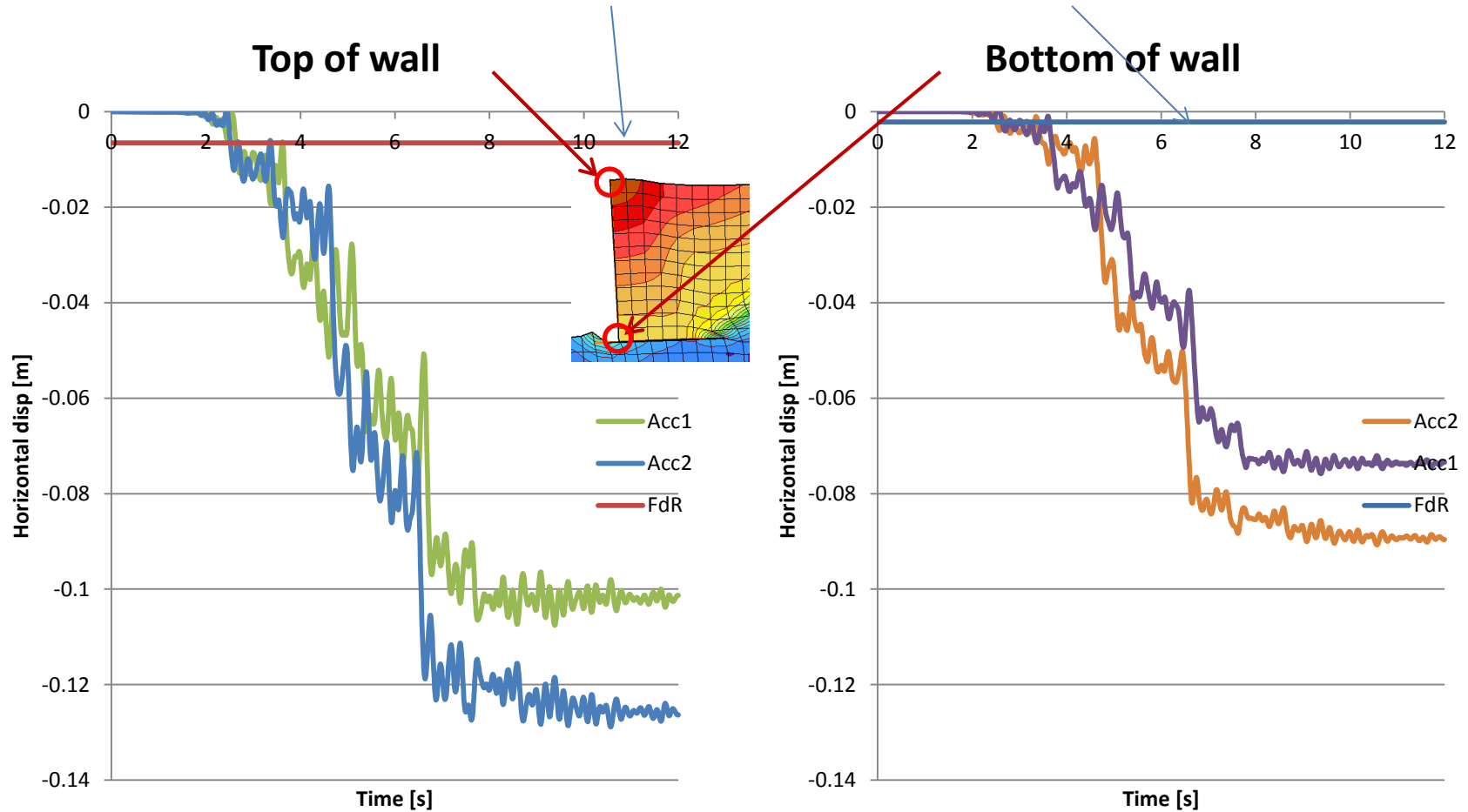
- Minimum 3 accelerogrammes (generated artificially, recorded at similar sites)
- 5 or more:
  - Mean + std.dev \* factor (e.g. Student-Fisher average)
- Fewer than 5:
  - Max/min values
  - If differences between accelerogrammes are big, consider selecting more accelerogrammes

# Wide footing, TH-analysis

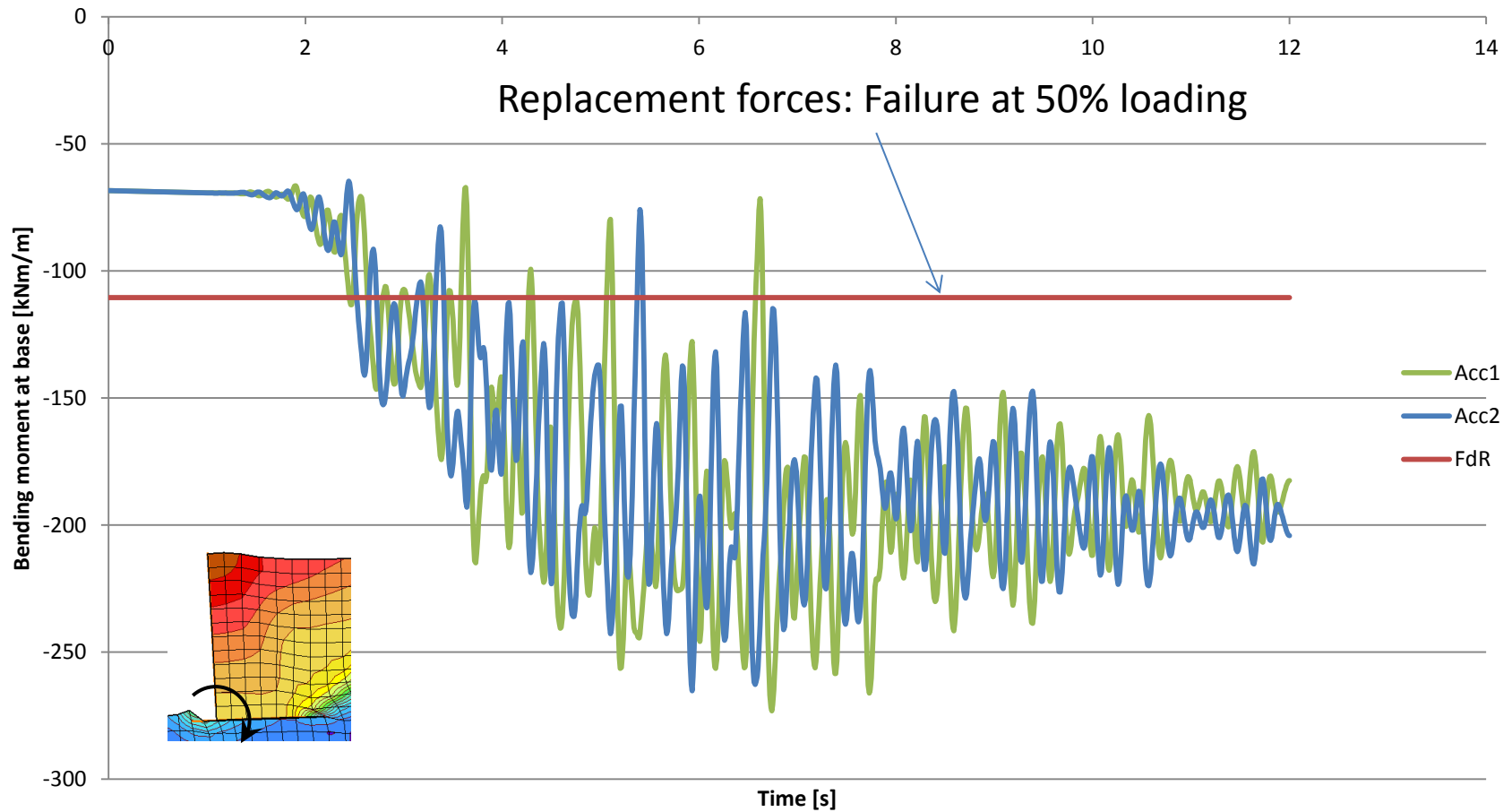


# Wide footing, displacements

Replacement forces: Failure at 50% loading

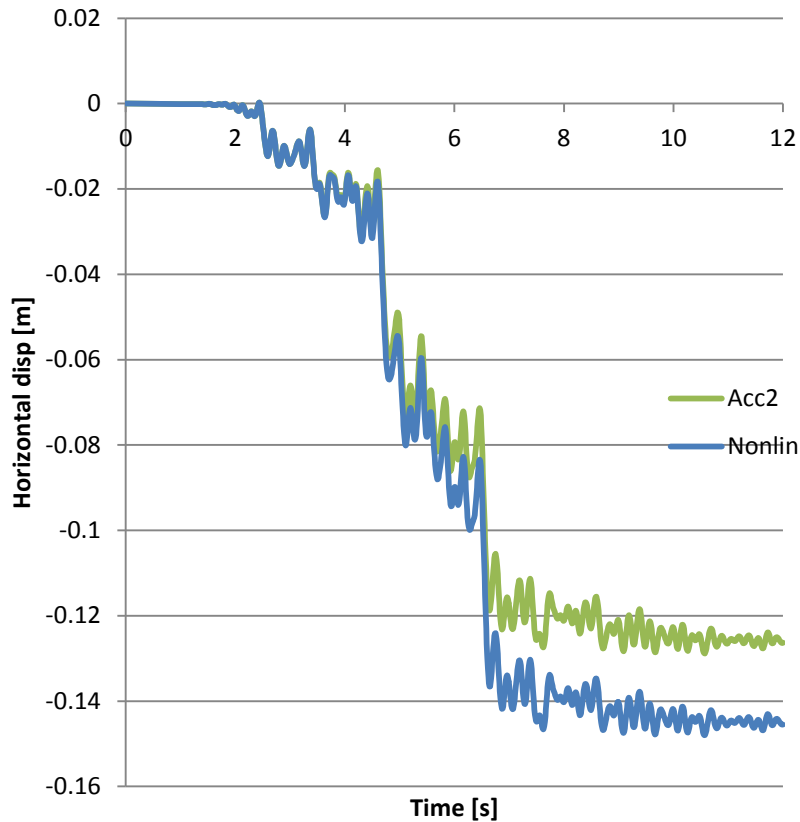


# Wide footing, bending moments

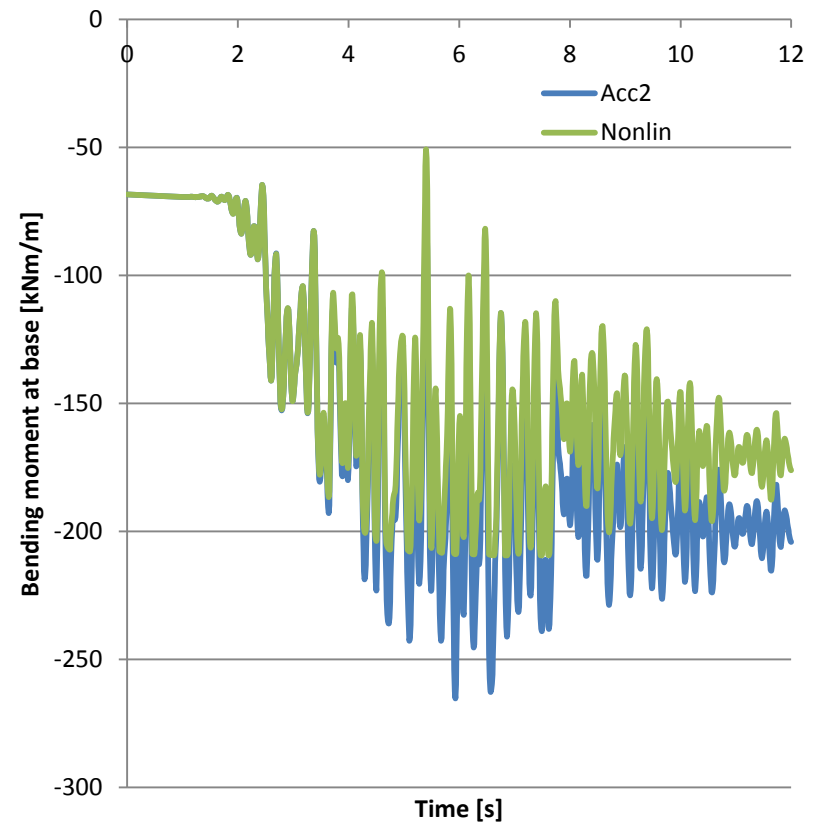


# El-pl retaining wall ( $M_{pl} = 210\text{kNm/m}$ )

## Displacement: Top of wall



## Bending moment at base



# Conclusions

- RF method is overly conservative
- TH is only method that correctly accounts for nonlinearities (plasticity, contact, nonlinear elasticity etc.)
- Zsoil is capable of computing TH for EQ-loading
  - All commonly used numerical tools are available
  - 2D models can easily be computed on laptop PC